References for
Recent Developments in Cluster-Robust Inference

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These references accompany the December 15 2021 webinar to the International Association for Applied Econometrics. They emphasize more recent research.

The webinar slides and recording will be available at https://appliedeconometrics.org/iaae-webinars

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