

**HOMEWORK # 1 (for due date see web page)**

Consider the following decision problem:

states →	$s_1$	$s_2$	$s_3$	$s_4$	$s_5$	$s_6$
acts ↓						
$a_1$	$z_1$	$z_2$	$z_3$	$z_4$	$z_5$	$z_6$
$a_2$	$z_7$	$z_8$	$z_9$	$z_{10}$	$z_{11}$	$z_{12}$
$a_3$	$z_{13}$	$z_{14}$	$z_{15}$	$z_{16}$	$z_{17}$	$z_{18}$

The agent’s ranking of the outcomes is as follows (where  $\succ$  means ‘better than’ and  $\sim$  means ‘just as good as’):

$$z_{15} \sim z_9 \succ z_{16} \sim z_{13} \sim z_7 \succ z_{10} \succ z_5 \succ z_{17} \sim z_6 \sim z_2 \succ z_{14} \succ z_8 \sim z_{18} \sim z_1 \succ z_3 \succ z_{11} \sim z_{12} \succ z_4$$

- (a) Represent the ranking by means of a utility function with values in the set  $\{1,2,\dots,9,10\}$
- (b) Re-write the decision problem replacing outcomes with utilities.
- (c) For every two acts, explain whether one dominates the other (and if so, state whether it is strict or weak dominance).
- (d) Find the Maximin solution.
- (e) Suppose now that, before deciding what to do, the agent learns that act  $a_3$  is no longer available and an expert informs the agent that, for sure, the state is not any of the odd-numbered ones (that is, the true state is one of  $s_2, s_4, s_6$ ). Find the Maximin solution of this reduced decision problem.